

24 We implemented SGSM++ to monitor for violations of 9 properties of
25 3 AVs from the CARLA Autonomous Driving Leaderboard, confirming the
26 viability of the framework, which found that the AVs violated 71% of prop-
27 erties during at least one test including almost 1400 unique violations over
28 30 total test executions, with violations lasting up to 9.25 minutes. Artifact
29 available at <https://github.com/less-lab-uva/ExtendingSGSM>.

30 *Keywords:* runtime verification, autonomous vehicles, safe driving
31 properties, scene graphs

32 1. Introduction

33 Autonomous vehicles (AVs) are quickly approaching wide-spread public-
34 road deployment, with several companies already leveraging fleets of AV taxis
35 in multiple US cities [1, 2]. However, deployments of full AV systems have led
36 to multiple human and animal fatalities [3, 4, 5, 6, 7]. While some analysis
37 from the companies deploying AVs suggests that they are involved in fewer
38 collisions that pose risk of injury compared to human drivers [8, 9], we con-
39 tinue to see AVs violate required driving behavior with grave consequences.

40 Ideally, AVs would be deployed without latent faults due to extensive
41 validation and verification [10, 11]. However, the inherent complexities of
42 these systems and the long-tail of potential scenarios make it infeasible to
43 provide complete and strong guarantees [12, 13]. These limitations have moti-
44 vated the use of runtime monitors that can evaluate compliance of safety
45 specifications during deployment [12, 13, 14, 15, 16]. However, current moni-
46 toring mechanisms are inadequate for checking driving behavior as they can-
47 not account for the spatiotemporal distribution of entities (e.g., other vehi-
48 cles, pedestrians, traffic signals) that may influence the AV driving behavior,
49 and which can only be obtained from complex multi-dimensional sensors like
50 camera and LiDAR. Alternatively, approaches that do account for driving
51 behaviors do it through bespoke, handcrafted translation between the moni-
52 tor’s input, e.g. sensor input, or internal system state, and the semantics
53 of the safety specifications, limiting generalizability (as per related work in
54 Section 2).

55 A key challenge with developing monitors for the driving behavior of
56 AVs is the mismatch between the semantic space over which typical road
57 properties are asserted (e.g., cars, stop lights, intersections) and the input
58 space of AVs which are typically in the form of sensed data (e.g., images,

LTL_f Formula for ψ_9 :

$$\mathcal{G}((\neg \text{hasStop} \wedge \mathcal{X} \text{hasStop}) \rightarrow (\mathcal{X}(\text{hasStop} \mathcal{U} (\text{isStopped} \vee \mathcal{G}(\text{hasStop}))))))$$

Atomic Propositions:

hasStop: $| \text{relSet}(Ego, \text{isIn}) \cap \text{relSet}(\text{stopLine}, \text{controlsTrafficOf}) | > 0$

isStopped: $| \text{filterByAttr}(Ego, \text{speed}, \lambda x: x < \varepsilon) | = 1$

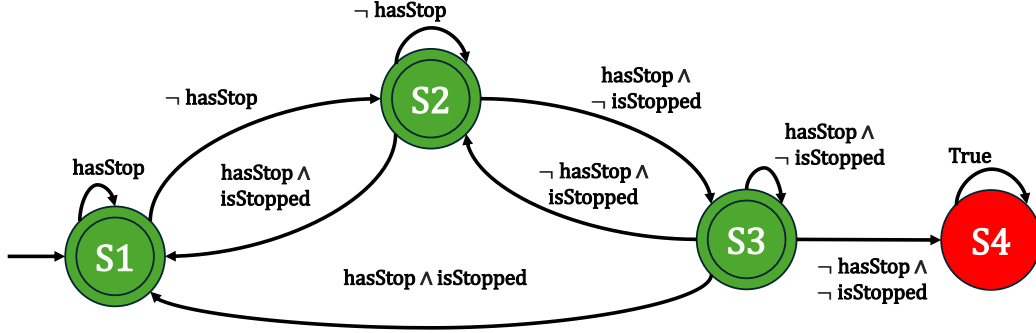


Figure 1: LTL_f for safe driving property, Atomic Propositions over the image sensor data, and DFA for property ψ_9 . Adapted from [18] for consistent notation.

59 radar, point clouds). As a motivating example, consider the following rule
 60 (ψ_9 in Table 1) from the Virginia Driving Code § 46.2-821 “*The driver of*
 61 *a vehicle approaching an intersection on a highway controlled by a stop sign*
 62 *shall, immediately before entering such intersection, stop at a clearly marked*
 63 *stop line [...]*” [17]. Evaluating this property requires extracting information
 64 about road lanes, stopping signals, e.g. stop signs, painted markers, etc.,
 65 which lanes the signals affect, and if the vehicle occupies those lanes.

66 To address these limitations we proposed utilizing scene graphs (SGs) to
 67 produce a framework for SG Safety Monitoring (SGSM) that enables the
 68 specification of driving properties for AVs and their automated synthesis as
 69 part of a system monitor. The approach builds on two key domain-specific
 70 components: 1) a spatial scene graph generator (SGG) that can extract rich
 71 scene representations from sensor inputs for the AV domain into SGs that
 72 abstract the entities related to the AV, and 2) a domain-specific language
 73 (DSL) that enables a developer to define programmable queries over the SG
 74 and compose the output of those queries as part of discrete metric temporal
 75 logic properties that can be monitored at runtime. Together, the SG and
 76 DSL offer a rich space to express common road properties relevant to AVs
 77 that can be automatically encoded as a runtime monitor.

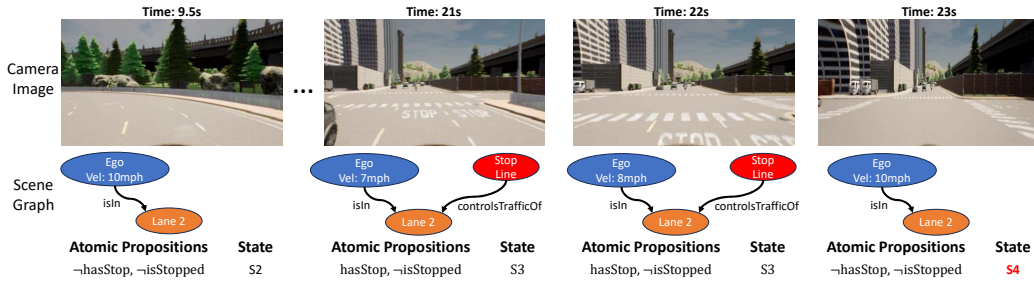


Figure 2: AV (TCP) running an intersection without stopping from [18]. Top: AV Camera Images. Middle: sub-SG for checking safety property. Bottom: Atomic Propositions evaluated from SG and updated state of the DFA shown in Fig. 1 leading to violation.

78 Our initial work in this area identified SGs as a useful abstraction for
 79 measuring test coverage for AVs at the semantic level [19]. That motivated
 80 our recent work introducing SGSMS [18] to leverage the semantic abstraction
 81 of SGs for safety monitoring. In this work, we extend and further elaborate
 82 SGSMS, producing SGSMS++. In this paper, we 1) provide additional detail
 83 and discussion on related works (Section 2) and SGSMS (Section 3), 2) extend
 84 the framework to SGSMS++ to enable tracking multiple violations including
 85 the number and duration of individual violations (Section 4), 3) provide a
 86 formal analysis of the expressiveness of the framework (Section 5), and 4)
 87 expand the experimental study to analyze the new contributions (Section 6).

88 Returning to the motivating example of a stop sign, Fig. 1 shows the safety
 89 specification described in linear temporal logic over finite traces (LTL_f) [20]
 90 (further discussed in Section 2.5), the atomic propositions (APs) expressed
 91 in our DSL, and the deterministic finite automaton (DFA) automatically
 92 synthesized from the LTL_f formula. Fig. 2 shows a snippet of a time sequence
 93 in which an AV passes an intersection controlled by a stop line without
 94 stopping. The top row shows the AV’s camera input, while the second row
 95 shows the subgraph of the SG relevant to the property extracted from each
 96 input image. As the AV approaches the intersection, the stop line appears in
 97 the graph with the relationship that it “controlsTrafficOf” the lane that the
 98 ego vehicle (ego from now on) is in; yet, ego’s velocity remains consistent.
 99 The APs and states shown at the bottom correspond to the transitions and
 100 state of the DFA at that time; note that as the input sequence progresses,
 101 and the stop line is included in the SG but ignored by the AV, the DFA
 102 moves toward and finally enters the failure state, S4, indicating a violation.

103 We introduce the first domain-cognizant, general, and extend-

104 **able approach for the specification of AV safety driving properties**
105 **that can be encoded for automatic monitoring during runtime.** The
106 approach is domain-cognizant in that it bridges the gap from raw sensor data
107 to primitive propositions that capture domain concepts. It is general in that
108 it is independent of the AV implementation, only requiring access to exter-
109 nal inputs and outputs, e.g. sensor data and AV control commands, from
110 which SGs can be derived. It is extendable in that the DSL building blocks
111 can be combined to encode properties beyond the ones we study. We imple-
112 mented the approach in CARLA [21] to explore its capabilities in simulation
113 for 3 AVs from the CARLA leaderboard competition. We find that these AV
114 systems, though highly performant under the existing competition metrics,
115 consistently violate driving rules—in 50% of executions the AV crossed into
116 opposing traffic (ψ_1) and in 73% of executions the AV ignored a stop sign
117 (ψ_9). Further investigation using SGS++ identified a combined 12.5s spent
118 in the opposing lane and 31 ignored stop signs in total.

119 **2. Background and Related Work**

120 We briefly survey related work in this area, including prior work on AV
121 safety monitors and ontologies for the AV domain, and work that is founda-
122 tional to our approach, including SGs to extract scene semantics, formula-
123 tions of propositions over graphs, and temporal logic to specify sequences of
124 proposition values.

125 *2.1. AV Safety Monitors*

126 Prior work has examined monitoring end-to-end systems. Desai et al.
127 propose using observable trajectories to monitor path following and safety
128 buffers using signal temporal logic (STL) [22]. Similarly, Zapridou et al. also
129 use STL to describe properties and check them using the CARLA simula-
130 tor [23]. Stamenkovich et al. use system-independent runtime monitors that
131 observe only the external inputs and outputs to check properties specified
132 in LTL [13]. Castelino et al. propose using vehicle communication systems
133 (V2X) to improve the robustness of runtime monitoring by the diversity of
134 available data [24]. Morse et al. characterize spatial relationships between
135 sensed objects and robot behaviors, by using graph representations and First
136 Order Logic (FOL), that can be used for runtime monitoring [25]. Similarly,
137 Matos Pedro et al. developed a runtime verification technique agnostic to the
138 target system for checking spatio-temporal properties using LTL and Modal

139 Metric Spaces [26]. Yalcinkaya et al. propose a runtime assurance framework
140 for programming AVs that emits a runtime monitor for the programmed be-
141 haviors [27]. Work in shielded reinforcement learning aims to learn [28] or
142 enforce [29] safety properties for agents specified in temporal logic and has
143 shown to increase robustness of learned behaviors.

144 However, each of the previous techniques assume there is a mapping
145 from the sensed inputs to the semantics of the atomic propositions (APs)
146 in their properties. Extracting the APs requires either limiting the proposi-
147 tions checked to those already consumed by the system or additional effort to
148 extract the relevant semantics, both of which limit its generalizability. In our
149 work we leverage Scene Graph Generators (SGGs), discussed in Section 2.3,
150 to generate the sensor input abstraction which we then process using our
151 domain-specific language to extract AP values, broadening the applicabil-
152 ity of our techniques to any system. Further, SGG is a burgeoning field of
153 study within machine learning and computer vision that is constantly ad-
154 vancing, with recent progress on SGGs showing improvements on research
155 benchmarks [30, 31]. This work provides the framework to benefit from these
156 improvements as we expect that the near future will bring faster, more ac-
157 curate, more broadly applied methods for SG generation which will further
158 broaden the applicability of our safety monitoring approach.

159 Prior work has also focused on building specialized monitors for AV soft-
160 ware subcomponents rather than full end-to-end systems, such as trajec-
161 tory prediction [32], collision avoidance [33, 34], lane changing and over-
162 taking [34, 35], or interfaces between AV components such as the CAN
163 bus [14, 36] or through ROS topics [37]. Additionally, most of these efforts
164 include propositions over simple types, e.g., “disengaged cruise control”, or
165 “traveled for 2 seconds”.

166 The introduction of machine-learned components to process multi dimen-
167 sional sensors complicates the design of monitors due to the black-box nature
168 of such components and their ability to perform what were previously sepa-
169 rate subtasks as end-to-end computations. Kochanthara et al. provide a ro-
170 bust characterization of component-level safety properties for the Apollo AV,
171 but do not explore methods for evaluating these properties at runtime [38].
172 Torfah et al. use counter-example guided learning to learn a runtime monitor
173 that can predict from an observed state if the AV is going to leave its safe
174 operation domain [39]. While this can learn to monitor for violations from ex-
175 amples, it cannot be used to encode a specific desired property a priori. Yang
176 et al. use a reachability analysis tool for runtime safety verification of a neu-

177 ral network navigation control system using LiDAR to avoid collisions [40];
 178 however, this is not generalizable to higher-order properties due to its narrow
 179 focus on control dynamics. Grieser et al. provide a mechanism for monitoring
 180 a limited set of safety properties based on LiDAR point clouds [41]. However,
 181 it is not generalizable to other sensors or properties because it is built around
 182 a DNN particularly tailored for this application that only takes in LiDAR
 183 points and outputs a torque value to control the motor and a steering angle
 184 command; different sensors or properties would require further bespoke con-
 185 figurations. Anderson et al. try to overcome this issue by introducing Spatial
 186 Regular Expressions for pattern matching over perception streams containing
 187 spatial and temporal data, leveraging object detection networks [42]; simi-
 188 larly, Balakrishnan et al. introduce PerceMon to monitor detection systems
 189 using specifications defined in TQTL [43]. Nonetheless, they can only reason
 190 about relationships given by bounding box overlap, and miss richer types of
 191 relationships like proximity between entities or traffic semantics. Similarly,
 192 Grundt et al. use STL to formally encode specifications, capturing physical
 193 attributes about the ego vehicle and the ego vehicle’s relationships to other
 194 vehicles, e.g. the angle of the ego vehicle or its distance to another vehicle.
 195 However, the formalism cannot capture semantic relationships nor relation-
 196 ships between other entities, fundamentally limiting the specifications that
 197 can be encoded [44].

198 *2.2. Ontologies for the AV Domain*

199 Another line of related research has explored different ontologies in the
 200 AV domain [45] for scenario-based testing [46, 47] and for situation as-
 201 sessment and decision making [48, 49, 50]. The main limitation of these
 202 approaches, however, is that the ontologies are completely tied to the SUT,
 203 thus only encoding the information needed by the system and making them
 204 nongeneralizable. Our previous work on SGs for AV testing [19] demon-
 205 strated the utility of SGs as a basis for measuring coverage of nontemporal
 206 properties, but does not provide a mechanism to express and automatically
 207 check the rich properties studied here. Closer to our abstraction, Majzik et
 208 al. envisioned using a graph-based ontology of the environment with STL to
 209 monitor system performance [51], but defines no properties for self-driving
 210 cars. Our work extends and formalizes this notion with: a spatial-relation
 211 graph that can be computed from external, system-independent inputs, a
 212 graph-semantics logic DSL and LTL_f that can specify safety-critical prop-
 213 erties; and we demonstrate that this approach can automatically find property

214 violations at runtime for AV driving systems.

215 2.3. Scene Graph Generation (SGG)

216 SGG is an emerging area of research focused on extracting relationships
217 between objects from sensor data, e.g., from an image input inferring a pedes-
218 trian is on a crosswalk. SGs are directed graphs [52], with a vertex set V that
219 represents the set of entities captured by a sensor, e.g., camera or LiDAR,
220 and a set of directed edges $(u, v) \in E$ describing their relationships. More
221 formally, an SG,

$$G = (V, E : V \mapsto V, Ego \in V, \\ kind : V \mapsto K, rel : E \mapsto R, att : V \cup E \mapsto M)$$

222 has a distinguished *Ego* vertex and functions to access the entity *kind* of
223 a vertex, the *relation* encoded by an edge, and *attribute* values of vertices
224 and edges. A map M is used to associate attribute values with each type of
225 attribute.

226 SGGs are highly configurable, enabling the SGs to be tailored to different
227 domains. SGGs can be configured to work with different parameterizations
228 based on the kinds of entities (K); e.g., whether cars and trucks should be
229 treated as separate classes, consolidated into a “vehicle” class, or ignored
230 completely. The types of relationships (R) captured and their semantics can
231 be configured based on the goals of the SGG; e.g., whether to include distance
232 information such as entities being “near” and “far” from each other or higher-
233 order information such as this lane “opposes” the other lane based on traffic
234 rules. The SGG parameterization extends to the attribute information (M),
235 e.g., whether to capture the color of the traffic light, the speed of the other ve-
236 hicle, or the height of the pedestrian. In recent years, many SGG techniques
237 have been developed [53] leveraging object detection systems (e.g. [54, 55])
238 to detect different entities, and then extract relationships between them. In
239 the realm of AVs, more tailored SGGs have been proposed [56, 57, 58], that
240 leverage domain-specific semantics like road types, vehicle types, and static
241 or dynamic entities. Our framework uses an SGG to extract graph-based
242 abstractions of sensor data from the world, and our study builds on an SGG
243 that operates in the CARLA AV simulator [21].

244 2.4. Graph Properties

245 There is a rich literature on methods for specifying properties of graphs.
246 Given the relational nature of graphs, properties could be specified as queries

247 in relational algebra [59] or in more specialized graph query languages built on
 248 relational algebra primitives [60, 61]. Using such methods one can formulate
 249 a wide range of property specifications. For example, one can express that
 250 “a graph contains a stop signal that controls the lane ego is in” by combining
 251 primitives relational *join* and set *intersection* as follows:

$$join(Ego, isIn) \cap join(stopsignal, controls) \neq \emptyset$$

252 where $stopsignal = \{v : v \in V \wedge kind(v) = stop\ signal\}$.

253 In this work, we focus on core primitives that can be used to specify prop-
 254 erties like the one described above. In addition to standard set operations,
 255 those primitives include join (relSet) and a primitive that allows selecting a
 256 subset of vertices based on properties of their attributes (filterByAttr), fur-
 257 ther discussed in Section 3.1.1. More complicated properties can be expressed
 258 over paths by composition and iteration using these primitives. Executable
 259 specifications built in this way are appropriate for runtime monitoring, in
 260 contrast to more declarative approaches [61].

261 2.5. Linear Temporal Logic

262 Linear Temporal Logic (LTL) is a formal language that has been widely
 263 used for modeling and analyzing systems with temporal aspects, including
 264 embedded and cyber-physical systems [62, 63, 64]. An LTL formula ψ , is sat-
 265 isfied by an infinite sequence of truth valuations of APs [65]. There are **logic**
 266 **operators**: *And* (\wedge), *Or* (\vee), *Not* (\neg), etc., and **temporal operators**: *Next*
 267 (\mathcal{X}), *Until* (\mathcal{U}), *Always* (\mathcal{G}), *Eventually* (\mathcal{F}). By leveraging these operators,
 268 LTL allows for the precise specification of the system’s behavior over time.
 269 For runtime monitoring, we use LTL over discrete, finite traces (LTL_f) [20].
 270 An LTL_f formula can be automatically converted to a DFA that validates
 271 whether a finite trace satisfies the property [66, 67] as shown in Fig. 1. Each
 272 DFA has a defined *start state* based on the LTL_f formula which will be used
 273 at the initial state when evaluating the formula. A given DFA may also have
 274 a *trap state*, a state whose only transitions are to itself such that regardless
 275 of the future AP values the DFA will remain in the trap state. LTL_f does
 276 not provide a language for specifying the APs themselves; rather, the APs
 277 must be evaluated before being consumed by the LTL_f formula.

278 3. SGSF Framework

279 Fig. 3 provides an overview of the monitoring framework which has two
 280 phases to enable the specification and runtime monitoring of driving proper-

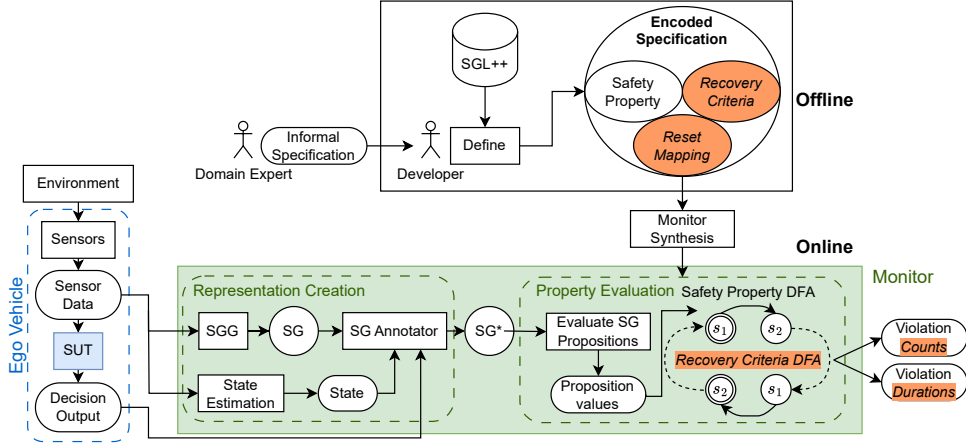


Figure 3: SGSM++ framework overview. SGSM++ offline phase at the top produces an encoded specification which is then synthesized into a monitor used in the online phase at the bottom to identify violations. Items in *orange italics* are part of the extension to SGSM++ (discussed in Section 4) from SGSM [18] (discussed in Section 3).

281 ties for AVs. First, in the offline phase shown at the top, a developer works
 282 to encode properties to be checked by the system. The encoded specification
 283 is then synthesized to produce a monitor which will evaluate each property
 284 during the online phase to monitor for property violations. In the online
 285 phase, the monitor leverages the sensor input and decision output of ego to
 286 create an enriched scene graph, SG^* , which is then used to evaluate the APs
 287 over SG^* to determine if a violation has occurred. Fig. 3 encompasses both
 288 SGSM, developed in our initial work [18], and further extensions explored in
 289 this work to create SGSM++. In Fig. 3, the novel components for SGSM++
 290 are shown in orange italics for clarity. The following sections provide further
 291 discussion on the SGSM framework; Section 4 then builds from this as the
 292 basis for the SGSM++ framework.

293 3.1. Offline

294 SGSM assists developers in formally specifying driving properties pre-
 295 pared by domain experts, such as those found in a driving manual, in a
 296 computable format that is checkable at runtime. The assistance comes in
 297 the form of a DSL, called Scene Graph Language (SGL), that allows the
 298 developer to define LTL_f formulas and evaluate propositions on the SG and
 299 ego’s state. The developer begins by encoding the specification as a safety

300 property in SGL, and defines the sampling rate at which the property needs
 301 to be checked. The safety property can then be synthesized into a system
 302 monitor that can be deployed during the online phase to check for property
 303 violations.

304 We now introduce SGL, which combines LTL_f and a set of SG querying
 305 functions, to facilitate the specification of driving properties.

306 3.1.1. Specification Definition

307 SGL allows the developer to reason about ego’s environment and state
 308 through propositions over sets of nodes in the SG. In addition to traditional
 309 set operations including union, intersection, and difference, SGL leverages
 310 two functions to perform graph queries: **relSet** and **filterByAttr**. Together,
 311 these functions will be used to derive sets of nodes with specific semantics,
 312 e.g., the set of red traffic lights. These sets will then allow for evaluating the
 313 atomic propositions by evaluating the elements of the set, e.g., whether or
 314 not there is a red traffic light is found by checking if the set of red traffic
 315 lights is non-empty.

316 The **relSet** function computes the join of a set of vertices and a relation.

$$\begin{aligned} relSet : (V_1 \subseteq V, r \in R) &\mapsto V_2 \subseteq V \\ V_2 &= \{v_2 : v_1 \in V_1 \wedge (v_1, v_2) \in E \wedge rel(v_1, v_2) = r\} \end{aligned}$$

317 For example, the set of lanes controlled by a stop sign is
 318 $relSet(stopSigns, controlsTrafficOf)$. SGL also supports **relSetR** – the join
 319 of the transpose of the given relation. The transpose allows, e.g., finding the
 320 set of stop signs that control a lane.

321 The **filterByAttr** function selects a subset of vertices, V_1 , whose at-
 322 tribute, m , satisfies a given predicate, f .

$$\begin{aligned} filterByAttr : (V_1 \subseteq V, m \in M, f : T \mapsto bool) &\mapsto V_2 \subseteq V \\ V_2 &= \{v : v \in V_1 \wedge type(att(v)[m]) = T \wedge f(att(v)[m])\} \end{aligned}$$

323 For example, $filterByAttr(trafficLights, lightState, \lambda x : x = Red)$ yields the
 324 corresponding set of red traffic lights. See Table 2 in Section 6 for SGL
 325 encodings of the atomic propositions evaluated for the properties studied.

326 As defined here, SGL utilizes only a core set of primitive operators, $relSet$
 327 and $filterByAttr$ as these, along with the set, logic, and temporal operators
 328 are sufficient for this application. This allows us to explore the benefit of the

329 approach with minimal language engineering and future work could build
 330 higher-level languages that compile to these core primitives. The study ex-
 331 amines in Section 6.2 the utility of this level of expression for its purpose as
 332 a runtime monitor.

333 SGL includes standard operators for numeric comparison, boolean logic,
 334 and set manipulation which are used to convert from vertex sets to APs.
 335 For example, whether ego has a throttle attribute below a given threshold,
 336 ϵ , is specified by $|\text{filterByAttr}(\text{Ego}, \text{throttle}, \lambda x : x < \epsilon)| = 1$. The APs are
 337 the building blocks for specifying different aspects of the AV’s environment
 338 and behavior and can be combined with temporal operators through LTL_f
 339 to express temporal relationships in the AV’s behavior, enabling a precise
 340 characterization of its actions and responses in dynamic environments.

341 SGL also builds on Linear Temporal Logic on Finite Traces (LTL_f) [20]
 342 which provides a set of logical and temporal operators (described in Sec-
 343 tion 2.5) for describing whether a finite trace of atomic proposition values
 344 satisfies the given LTL_f formula. For example, Fig. 1 shows the LTL_f for-
 345 mula for ψ_9 which encodes that the AV must stop at stop signs. Informally,
 346 this formula states that always, once the AV detects a stop sign, it must
 347 detect the stop sign until it has stopped; i.e., if it stops detecting the stop
 348 sign without having stopped, then it has run the stop sign. Section 4.1.2
 349 provides additional, precise discussion of ψ_9 ’s LTL_f encoding.

350 In addition to the standard temporal operators, SGL also defines a dis-
 351 crete metric operator, $\$[N][\text{AP}]$, to ease the LTL_f specification over repeated
 352 APs by unrolling the AP N times using the \mathcal{X} operator. Under a set sam-
 353 pling rate, this can be used to specify, e.g., that an AP has a certain value
 354 for a certain duration. This is studied in Section 6 for properties that check
 355 that the ego vehicle completes an action within a certain time window. We
 356 also adopt the use of the `last` keyword from prior work as a shorthand for
 357 $\neg \mathcal{X} \text{ True}$ which encodes intuitively that the current input must be the last
 358 input—all future inputs lead to the formula not accepting [20].

359 3.1.2. Monitor Synthesis

360 The foundation of all SGL specifications is the safety property encoding
 361 to enable the synthesis of the monitor. The property must be encoded as a
 362 safety constraint, i.e. a property that must be continuously satisfied during
 363 execution. The formula will be evaluated repeatedly at runtime by the mon-
 364 itor and thus it must be specified in such a manner so that all satisfactory
 365 sub-traces are also accepting. In the corresponding DFA for the LTL_f for-

366 mula this means there must be a unique non-accepting state and that state
367 must also be a trap state. This is exemplified by the property ψ_9 shown in
368 Fig. 1; examining the DFA, we see that there are three accepting states that
369 correspond to the progression of the LTL_f formula, and a unique failure state
370 that is also the trap state.

371 The correctness of the synthesized monitor is predicated on maintaining
372 a consistent state between the monitor and the system. While this warrants
373 careful consideration in the construction of the whole encoding, particular
374 care is required setting the start state during initialization to reflect the
375 state of the system. This could be enforced through outside guarantees of
376 the system being in a known state at the start of monitoring, or by the
377 encoding assuming no particular initial state and using the APs during the
378 first several time steps to identify a known state being reached.

379 3.2. Online

380 As ego senses the environment, it provides data to the system under
381 test (SUT) to produce a decision output for the vehicle. SGSM provides a
382 runtime monitor (green box) to check for property violations by processing
383 sensor data and appending the ego’s decision output to create SG^* . It then
384 evaluates the SGL function over SG^* to assign the values of the APs. These
385 AP values are then used to update the LTL_f DFA state machine. Finally,
386 the monitor outputs if the property holds or is violated based on the DFA
387 state. The monitor has two main modules described next.

388 3.2.1. Representation creation

389 This module consumes sensor data to estimate the state of ego and to
390 produce an SG through the SGG component. The resulting SG is enriched
391 by the SG annotator component with information about the SUT’s output,
392 and the state of ego to produce SG^* . For example, Fig. 2 shows the relevant
393 subgraphs generated for evaluating ψ_9 to monitor for stop sign violations. As
394 shown in the middle two time steps, the SG contains ego in lane 2 as well as a
395 stop line that controls lane 2. This information can be readily computed from
396 ego’s external sensor input to perceive which lane it is in and the presence
397 of a stop signal, perhaps in combination with available high-definition maps.
398 Additionally, the ego node contains an attribute for its velocity which could
399 be measured from its speedometer, etc. to check if ego is stopped. Though
400 not used in this example, SG is also annotated with ego’s decision output to
401 produce SG^* . We can imagine a related property to ψ_9 that instead stated

402 that immediately after detecting a stop signal, ego must begin to decelerate—
403 this could be monitored by checking that ego immediately output a sufficient
404 brake command.

405 In this presentation, SGSMS aims to monitor for property violations that
406 occur in the world. As such, the creation of SG^* is designed to be black-
407 box with respect to the SUT to maximize the generality of the approach,
408 only using externally observable sensor data, i.e. SUT inputs, and decisions,
409 i.e. SUT outputs. However, SGSMS could also be employed in a white-box
410 fashion to monitor the internal components of the SUT. For example, the
411 SG annotator could additionally enrich SG^* to include information from the
412 motion planning or control components of the SUT to allow for specifying
413 safety properties over, e.g., the planned future trajectory of the AV. We leave
414 the exploration of such properties for future work.

415 3.2.2. Property evaluation

416 This module takes in SG^* and an SGL function containing the LTL_f
417 property. It first evaluates each AP by querying SG^* , and then uses the AP
418 values to update the DFA state. Depending on the DFA state, the monitor
419 returns whether the property holds or is violated.

420 Table 3 gives a complete list of APs computed to evaluate the properties
421 studied. These APs yield an understanding of the spatial and temporal
422 distribution of entities related to ego. For example, ψ_9 checks if ego responds
423 to stop signs by evaluating the *hasStop* and *isStopped* APs. *hasStop* is true
424 iff the set of lanes controlled by stop signs and lines (*stopSignLanes*) intersect
425 with the set of lanes ego is in (*egoLanes*) is non-empty, which would indicate
426 that ego is being directed to stop. *isStopped* is true iff the set of ego with
427 speed $< \epsilon$ (*egoStopped*) is non-empty, indicating that ego is stopped.

428 4. Extending SGSMS

429 We will first introduce the challenges to SGSMS and then introduce two
430 extensions to address them.

431 4.1. Motivation

432 We now explore the limitations of SGSMS as presented across two dimen-
433 sions. First, the properties as encoded in SGL differ from those encountered
434 in, e.g., the driving code in one crucial dimension: the ability to handle mul-
435 tiple violations, i.e. to count the number and duration of different violations.

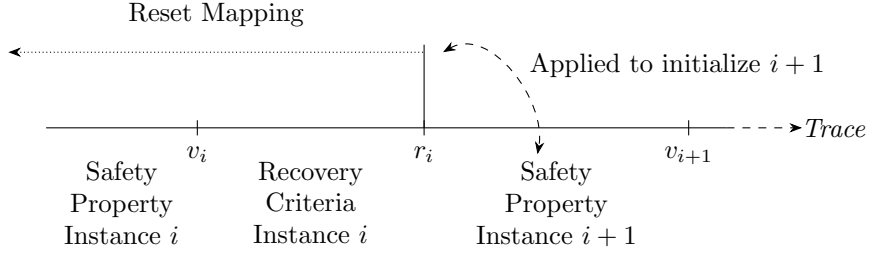


Figure 4: Timeline diagram, time advancing left to right, illustrating the use of SGSM++ to identify the start of a violation at time v_i , its recovery at time r_i , and the initialization of a the safety property to monitor future violation v_{i+1} .

436 Second, we consider the impact of extensions in this direction on how the
 437 properties’ initializations are encoded.

438 At a high level, Fig. 4 illustrates the timeline of a trace of an AV system
 439 being monitored for violations of a safety property specified in LTL_f . At time
 440 v_i , the i^{th} property violation is identified. In order to count future violations,
 441 a recovery criteria specified in LTL_f begins monitoring to determine when
 442 the violation has concluded, which eventually occurs at time r_i . Once the
 443 recovery formula has been satisfied, the approach must reset the safety prop-
 444 erty to enable monitoring. However, the conditions that are present at the
 445 time of reset may be different from the initial conditions that were assumed
 446 by the system and property when monitoring began. To address this, a reset
 447 mapping specified in LTL_f is provided that captures the relevant subset of
 448 the trace history and uses it to initialize the safety property monitor. This
 449 paradigm allows for identifying multiple violations of a property over a single
 450 trace and by examining the timing of the violations and subsequent recover-
 451 ies, the number of total violations and the duration of each violation can be
 452 calculated. The following sections briefly motivate and describe this process
 453 in more depth.

454 4.1.1. Counting and Duration

455 Consider ψ_9 shown in Fig. 1, the original specification from the driving
 456 code, § 46.2-821 says “[a] vehicle approaching an intersection on a highway
 457 controlled by a stop sign, shall, immediately before entering such intersection,
 458 stop [...] before entering” [17]. Though not specified, this specification implic-
 459 itly applies over *each* intersection that the vehicle approaches. However, it is
 460 encoded in SGL as $\mathcal{G}((\neg hasStop \wedge \mathcal{X}(hasStop)) \rightarrow (\mathcal{X}(hasStop \mathcal{U} (isStopped \vee$

461 $\mathcal{G}(\text{hasStop}))$), which says that *globally* (\mathcal{G}), the vehicle must never run a
462 stop sign. This difference between “for each intersection” and “globally for
463 all intersections” leads to different behaviors after the first violation. Un-
464 der the encoding, once any stop sign has been passed without stopping, the
465 vehicle is in violation, and it cannot recover from this violation, in effect
466 resulting in no additional monitoring for future stop signs. We can imagine
467 a meta-property stating that the vehicle can run no more than N stop signs;
468 for fixed N , this can be encoded by chaining the inner terms of ψ_9 , but this
469 cannot monitor for an unbounded number of violations.

470 Further, some violations lend themselves to a notion of “duration of viola-
471 tion”. Consider § 46.2-804 (ψ_1) which states “Wherever a highway is marked
472 with double traffic lines consisting of two immediately adjacent solid yellow
473 lines, no vehicle shall be driven to the left of such lines” [17]. This is en-
474 coded as $\mathcal{G}(\neg isOppLane)$ to denote that globally the vehicle should not be
475 in the opposing lane. Even with the ability to count the number of times
476 that the vehicle is in the opposing lane, we may additionally want to track a
477 qualitatively different metric capturing the *duration* that the vehicle was in
478 violation, e.g. the amount of time spent in the opposing lane. Under SGL,
479 for specific durations of interest, different parameterizations of the property
480 could be encoded to track, e.g., spending less than 1 second or 10 seconds in
481 the opposing lane, but with finitely many properties there is a strict bound
482 on the number of distinct durations that can be tracked.

483 This work extends the expressiveness of SGL to handle both counting
484 and duration tracking in Section 4.2.

485 4.1.2. Handling Re-initialization

486 As noted in Section 3.1.2, the correctness of the monitor is predicated
487 on maintaining a consistent state between the monitor and the state of the
488 system. This is particularly critical when the monitor is initialized; either
489 external guarantees must be in place to ensure that the system and moni-
490 tor are in a consistent initial state, or the safety property encoding must be
491 specified so as to not assume a particular prior state, i.e. it must initialize
492 into a “warm up” period where it observes the trace until it can reach a
493 known state. For example, if the AV always begins in a set location such
494 as a parking garage with known characteristics, the safety property could
495 use this assumption in its initialization; by contrast, if there exists a possi-
496 bility that the monitor is not enabled until the AV is mid-deployment, no
497 such assumptions can be made. Controlling for this initialization can im-

498 pact the semantics of the encoded safety property. Consider ψ_9 , the original
 499 specification from the driving code, §46.2-821 says “[a] vehicle approaching
 500 an intersection on a highway controlled by a stop sign, shall, immediately
 501 before entering such intersection, stop [...] before entering” [17]. However,
 502 the natural language description shown in Table 1 says “once the ego vehicle
 503 detects a *new* stop signal controlling its lane, it must stop before passing
 504 the stop signal”. The word “*new*” is added because the specification cannot
 505 make any assumptions at initialization. It is possible that at the time the
 506 safety monitor is enabled there is a stop sign already present. In such a case,
 507 the AV may have stopped prior to the safety monitor being enabled; given
 508 this uncertainty, the developers must decide which way to err in implementa-
 509 tion: either require the AV to stop, potentially in excess of what is required,
 510 or do not require the AV to stop at the first stop sign, potentially missing
 511 a violation. The implementation of ψ_9 chooses the latter, only requiring the
 512 AV to stop at *new* stop signs. As such, the start state is incorrect to serve
 513 as the initial state for reinitialization to monitor for future violations; once
 514 a violation has occurred, we know from the history of the scenario that ego
 515 should stop for the next stop sign as it definitely has not stopped for it in the
 516 past. This highlights how the initial state at monitor startup and the initial
 517 state of the monitor when being reset to observe for additional violations
 518 may need to be different. We refer to the initial state for future monitors as
 519 the *reset state*.

520 From this understanding of ψ_9 , we can then ascribe semantics to each of
 521 the four DFA states shown in Fig. 1. We will use this running example to
 522 better understand the solution described in Section 4.3.

523 S1: (*accepting*) The AV is controlled by a stop sign but either has already
 524 fulfilled its obligation to stop or does not need to stop because the stop
 525 sign was already present at initialization.

526 S2: (*accepting*) The AV is not controlled by a stop sign.

527 S3: (*accepting*) The AV is controlled by a stop sign and has not yet fulfilled
 528 its obligation to stop.

529 S4: (*failure; trap*) The AV was controlled by a stop sign and did not stop
 530 before it stopped being controlled by a stop sign.

531 4.2. Recovery Criteria Encoding

532 As discussed, the safety property encoding of a SGL specification must
 533 have a unique failure/trap state. In order to count the duration and number

Algorithm 1 SGSM++ violation and duration counting

```

1: procedure VIOLATIONCOUNTDURATION(propDFA, recoveryDFA)
2:   currTime  $\leftarrow$  0
3:   violationStarts  $\leftarrow$  {} ▷ Track violation start times
4:   violationEnds  $\leftarrow$  {} ▷ Track violation end times
5:   ▷ Violation start/end time yields count, duration, and timing info
6:   inViolation  $\leftarrow$  False
7:   while isRunning do
8:     currentState  $\leftarrow$  evalAPs(getCurrSG()) ▷ Update APs from SG
9:     propDFA.step(currentState) ▷ Step the property DFA
10:    ▷ Violation means trap state, is safe to keep stepping
11:    if  $\neg$ propDFA.isAccepting() then ▷ In violation
12:      if  $\neg$ inViolation then
13:        violationStarts.push(currTime) ▷ Mark violation start
14:        inViolation  $\leftarrow$  True
15:        recoveryDFA.step(currentState) ▷ Step the reset DFA
16:        if recoveryDFA.isAccepting() then ▷ Violation ended
17:          inViolation  $\leftarrow$  False
18:          violationEnds.push(currTime) ▷ Mark violation end
19:          propDFA.reset() ▷ See Section 4.3
20:          recoveryDFA.reset()
21:        currTime  $\leftarrow$  currTime + 1
22:      ▷ If ending in violation, there will be an unmatched start time
23:  return violationStarts, violationEnds

```

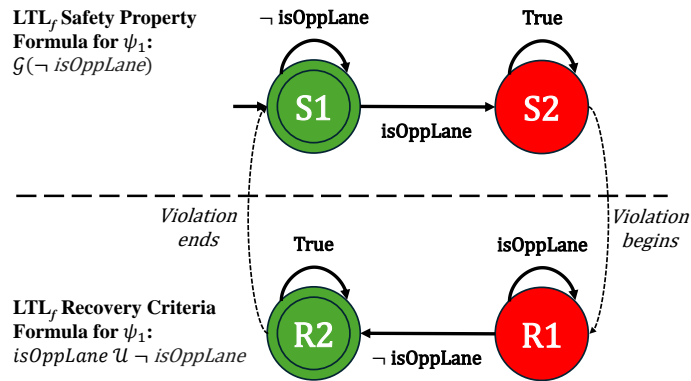


Figure 5: LTL_f for ψ_1 and its recovery criteria

534 of violations, there must be a way to exit the trap state. For this, SGSM++
 535 uses a *recovery criteria* that specifies when the safety property DFA should
 536 exit the trap state.

537 Algorithm 1 provides a pseudocode outline of this procedure; we refer to
 538 the line numbers in this algorithm in the following explanation. The recovery
 539 criteria expresses, through LTL_f , that acceptance only occurs when the AV
 540 has stopped violating the safety property. Once the safety property DFA
 541 has entered the non-accepting state which is also the trap state (line 11),
 542 SGSM++ marks the start of a new violation (line 13) and begins evaluating
 543 the recovery criteria LTL_f formula (line 15). Once the recovery criteria DFA
 544 accepts (line 16), the end of the violation is marked (line 18) and the safety
 545 property DFA is reset (line 19); more information about how that reset is
 546 performed is explained in the next section. In this paradigm, converse to the
 547 safety property encoding, the corresponding DFA for the recovery criteria
 548 must have a unique *accepting* state that is also the trap state. The reset
 549 DFA is also reset once it accepts (line 20). As shown in Algorithm 1, the
 550 implementation tracks the start and end of every violation which can be
 551 used to determine the count and duration. This process is visualized in the
 552 timeline shown in Fig. 4 where the safety property DFA is evaluating until
 553 the violation is identified at time v_i , when the recovery criteria DFA begins
 554 evaluating until the end of the violation is identified at time r_i . The duration
 555 of the violation is thus $r_i - v_i$.

556 For example, ψ_1 specifies that the vehicle cannot be in the opposing lane
 557 and the safety property is encoded as $\mathcal{G}(\neg isOppLane)$. The recovery criteria
 558 for ψ_1 is that the vehicle no longer be in the opposing lane, which is encoded
 559 as $isOppLane \mathcal{U} \neg isOppLane$; that is, evaluation continues as long as the AS
 560 continues to be in the opposing lane and only accepts when this is no longer
 561 the case. This paradigm generalizes; all specifications of the form $\mathcal{G}(\neg a)$ have
 562 a natural recovery criteria of $a \mathcal{U} \neg a$. Fig. 5 illustrates this case through the
 563 safety property DFA (top) and the recovery criteria DFA (bottom). During
 564 monitoring, the safety property DFA begins in state S1 and stays as long
 565 as $isOppLane$ remains *True*. Once $isOppLane$ is *False*, the safety property
 566 DFA transitions to S2. As this is the non-accepting trap state, execution
 567 immediately passes to the recovery criteria DFA and the start of a violation
 568 is recorded. The recovery criteria DFA starts in state R1 and will remain in
 569 this non-accepting state until $isOppLane$ is *False*, at which point the recovery
 570 criteria DFA will transition to R2 and execution immediately passes to the
 571 safety property DFA and the end of the violation is recorded.

572 The default recovery criteria is *False*, meaning that the specification is
573 irrecoverable. In this way, we can model the properties explored in prior
574 work on SGSM as having a recovery criteria of *False* which is strictly weaker
575 in terms of expressiveness [18]. Under previous work it was not possible to
576 count the number and duration of violations, only whether or not a violation
577 occurred at least once during the trace.

578 By contrast to irrecoverable specifications, some specifications are in-
579 stantly recoverable, i.e. there is no sensible concept of “duration of viola-
580 tion”. Consider ψ_9 which captures the specification that the AV should not
581 run a stop sign. There is no sensible concept for the duration of running
582 the stop sign—once the AV has passed the stop sign it cannot recover *for*
583 *that stop sign*; however, it is still useful to track future violations, i.e. fu-
584 ture stop signs. In these cases, the recovery criteria is trivial—a criteria of
585 *True* means that the recovery is instantaneous and v_i equals r_i . As shown
586 in Algorithm 1, this will result in the violation start and end being marked
587 during the same iteration through the while loop since the recovery DFA is
588 immediately accepting.

589 4.3. Reset Mapping Encoding

590 As noted in Section 4.1.2, the behavior of the safety property must make
591 decisions about how to handle the initialization of the monitor to ensure
592 the system and monitor are in a consistent state. This poses a challenge
593 when resetting the property; a naive implementation could restart the safety
594 property DFA at its start state as it would be during monitor start up.
595 However, at the time of reset there is a known history that led to the violation
596 or its recovery, and so restarting at the initial state of the safety property
597 may not be correct. In the example of ψ_9 , the developer may choose to be
598 lenient in the encoding of the property to not enforce the desired behavior
599 until a known state is reached, namely that there are no stop signs so that
600 is guaranteed that the AV must stop for any *new* stop signs.

601 From the discussion on ψ_9 in Section 4.1.2, state S2 is the only accepting
602 state that corresponds to the AV not being controlled by a stop sign. This
603 is precisely the known state of the system when the violation occurs—a vio-
604 lation means that the AV is no longer controlled by a stop sign. Thus, the
605 correct behavior is to reset to state S2 rather than S1 as we can reason about
606 the semantics of the violation behavior to understand how the prior history
607 informs future potential violations, ensuring that the system and monitor
608 are in a consistent state. It is important to note that not all aspects of the

609 history are useful. In this case, the history of the *hasStop* variable is critical
610 to understanding the known state of the environment for future potential
611 violations; however, the *isStopped* variable's history is not useful as we need
612 to ignore the history of the violation in order to reset to track for future
613 violations. From this understanding that violating ψ_9 guarantees a known
614 history of the AV not being controlled by a stop sign, SGSM++ provides
615 the user with a mechanism to specify what portion of the history should be
616 applied to the future monitoring.

Algorithm 2 SGSM++ reset mapping encoding

```

1: procedure FINDRESETSTATE(propDFA, resetDFA)
2:   productDFA  $\leftarrow$  cartesianProduct(propDFA, resetDFA)
3:    $\triangleright$  Remove the unsatisfiable transitions
4:   for transition  $\in$  productDFA.transitions() do  $\triangleright$  Over propDFA  $\wedge$  resetDFA
5:     predicate  $\leftarrow$  transition.predicate()
6:     if unsat(predicate) then
7:        $\lfloor$  productDFA.removeTransition(transition)
8:      $\triangleright$  Iteratively prune unreachable states
9:   repeat
10:    prevProductStates  $\leftarrow$  |productDFA.states()|
11:    for productState  $\in$  productDFA.states() do
12:      if isUnreachable(productState) then
13:         $\lfloor$  productDFA.remove(productState)
14:    until prevProductStates == |productDFA.states()|
15:     $\triangleright$  Find accepting states
16:    acceptingStates  $\leftarrow$  {}
17:    for (propState, resetState)  $\in$  productDFA.states() do
18:      if resetState.isAccepting() then
19:         $\lfloor$  acceptingStates.add(propState)
20:    if |acceptingStates| == 0 then
21:      RaiseError: reset mapping over-constrains history
22:    else if |acceptingStates| > 1 then
23:      RaiseError: reset mapping under-constrains history
24:    else
25:       $\lfloor$  return acceptingStates.pop()

```

617 The user specifies the relevant history by providing a *reset mapping* as an
618 LTL_f formula that accepts on exactly the possible histories that inform the
619 known state of the system at the end of the violation. The reset mapping is
620 used to identify which state in the safety property DFA should be used as
621 the reset state as shown in Algorithm 2. In Fig. 4, this is shown above the
622 trace; it is assumed that the reset mapping is accepting at the time that the

623 recovery criteria is accepting and that the history that led to this acceptance
624 provides the information needed to reset the monitor into a state that is
625 consistent with the system. Note that the default reset mapping $\neg\mathcal{F}$ **last**,
626 which only accepts on the empty trace, always results in the reset state being
627 the same as the original start state. This fits our intuitive understanding, as
628 this says that there is no particular history that is relevant to the reset.

629 First, the cartesian product of the safety property DFA and the reset
630 mapping DFA is computed (line 2). Then, edges which are logically unsatis-
631 fiable are removed (lines 4-7). Finally, all unreachable states are iteratively
632 pruned from the resulting DFA (lines 9-14). To find the reset state of the
633 safety property DFA, create an empty set (line 16); then for each state in the
634 product graph that corresponds to an accepting state in the reset mapping
635 graph, add the corresponding safety property state to the set (lines 17-19).
636 If the provided reset mapping is valid, this will result in a set of exactly
637 one state (lines 24-25); if the set is empty (line 20-21) or has more than one
638 state (lines 22-23), then the provided reset mapping is not valid for the safety
639 property because it either over-constrains or under-constrains the set of pos-
640 sible histories such that their application to the safety property state either
641 resulted in no possible states or multiple possible states. This algorithm is
642 run only once at compile time during monitor synthesis and the found reset
643 state is stored for use during online monitoring.

644 In the case of ψ_9 , the desired history captures that in the past ego was
645 controlled by a stop sign until the latest time step when ego was no longer
646 controlled by a stop sign. This is encoded as *hasStop* $\mathcal{U} (\neg\textit{hasStop} \wedge \textit{last})$;
647 note the use of the **last** keyword to denote end of input as discussed in
648 Section 3.1.1. Running this algorithm on ψ_9 using the reset mapping given
649 above results in state S2 being identified as the reset state as expected.

650 5. Limitations of Expressiveness

651 Although the extension from SGSM to SGSM++ has increased the ex-
652 pressiveness of the approach and enabled the monitoring of additional prop-
653 erties and multiple violations, the set of all possible properties is large. We
654 now reflect on the limitations of SGSM++ with respect to its expressiveness
655 and accuracy.

656 *5.1. Temporal Properties over Symbolic Entities*

657 As described in Section 3.2, at each time step the online portion of the
 658 framework occurs in two phases: first the AP values are extracted from the
 659 current SG, and then these AP values are used to drive the DFA update.
 660 This strict boundary between the evaluation of the AP and any temporal
 661 information limits the expressiveness of SGSM++ due to not being able to
 662 propagate relevant information through time. Consider § 46.2-820 which
 663 states “[...] when two vehicles approach or enter an uncontrolled intersection
 664 at approximately the same time, the driver of the vehicle on the left shall
 665 yield the right-of-way to the vehicle on the right” [17]. In order to encode
 666 this specification, we must have information about when ego approaches an
 667 intersection and when another vehicle approaches an intersection in order to
 668 know if those two actions happen at the same time. A single instance of this
 669 interaction could be imagined in LTL_f as:

$$\begin{aligned}
 & (\neg egoAtIntersection \wedge \neg otherVehicleAtIntersection) \wedge \\
 & \mathcal{X}(egoAtIntersection \wedge otherVehicleAtIntersection \\
 & \quad \wedge egoOnLeftOfOtherVehicle) \\
 & \quad \rightarrow \\
 & \mathcal{X}\mathcal{X}(egoAtIntersection \mathcal{U} \neg otherVehicleAtIntersection)
 \end{aligned}$$

670 That is, if ego and the other vehicle begin not at the intersection in the
 671 first time step, then at the second time step they are both at the intersec-
 672 tion and ego is on the left, then until the other vehicle leaves the intersec-
 673 tion, ego must continuously wait at the intersection. While the value for
 674 *egoAtIntersection* can be directly observed from ego’s state and surround-
 675 ing, determining *otherVehicleAtIntersection* under this context requires not
 676 just determining that *some* vehicle is at the intersection at each time step,
 677 but that *the same vehicle* is at the intersection for each of these evaluations.
 678 This notion of the same vehicle cannot be expressed in general by SGL using
 679 the graph querying functions described in Section 3.1.1—either the specifi-
 680 cation can be encoded to check for some vehicle by using the entity kind
 681 filter, e.g. $otherCars = filterByAttr(G \setminus \{Ego\}, kind, \lambda x : x = car)$ to say
 682 that some car but not necessarily the same car each frame is at the intersec-
 683 tion, or it can check for a specific car by using a unique identifier attribute,
 684 e.g. $car01 = filterByAttr(otherCars, uniqID, \lambda x : x = car01)$ to say that ego

685 should yield to `car01`¹. Checking for just some vehicle without guaranteeing
686 that all parts of the equation refer to the same vehicle at all time steps is log-
687 ically incorrect. Checking for a specific vehicle using a unique identifier will
688 check the correct behavior, but only for the specific vehicle hard-coded into
689 the property. As such, the specification cannot be checked in the general case
690 for yielding to arbitrary vehicles and can only be checked for a predetermined
691 set of identifiers. This comes from the inability to transfer this additional
692 context information through time as only the truth values of the APs can be
693 transferred through time using the LTL_f formula. A more accurate encoding
694 of the property can be imagined as follows—note that the vehicle quantifier
695 binds across time.

$$\begin{aligned}
& \forall vehicle : \{(\neg egoAtIntersection \wedge \neg atIntersection(vehicle)) \wedge \\
& \quad \mathcal{X}(egoAtIntersection \wedge atIntersection(vehicle)) \\
& \quad \wedge egoOnLeftOf(vehicle)) \\
& \quad \rightarrow \\
& \quad \mathcal{X}\mathcal{X}(egoAtIntersection \mathcal{U} \neg atIntersection(vehicle))\}
\end{aligned}$$

696 In this way, such properties require a *symbolic entity* so as to not only
697 evaluate that the property holds, but over which other vehicles. This may
698 be achievable by instantiating separate monitors based on the product space
699 of the quantifiers as this has been successful for other runtime monitoring
700 tasks [43]. However, further work is required to demonstrate that this re-
701 mains efficient to meet runtime constraints as prior work is exponential in
702 the number of quantifiers. A key benefit of SGSM++ is that it runs in
703 constant time and even with this limitation has demonstrated the ability to
704 encode important safety properties. While we characterize this limitation,
705 we leave its solution to future work.

706 5.2. Monitoring over Discrete Time

707 A fundamental limitation of the SGSM++ framework comes from its use
708 of discrete evaluations of the properties and underlying APs in time. While
709 a sufficiently rich logic could leverage continuous time, in practice SGs can

¹The ability to produce a consistent unique identifier is itself a hard problem with ongoing research, referred to as “object reidentification” [68, 69, 70] or “object tracking” [71, 72] in the literature.

710 only be implemented over discrete time. This can be mitigated by increasing
711 the rate at which a property is evaluated, but this will always impact the
712 semantics of the implemented monitor. For example, consider ψ_1 saying ego
713 must not be in the opposing lane. Once an SG is observed where ego is in the
714 opposing lane, the duration of violation is measured until an SG is observed
715 where ego is not in the opposing lane. If ego returned to its own lane and
716 then re-entered the opposing lane between the time two successive SGs were
717 captured and evaluated, then what to the system was two violations appear
718 to the monitor as one longer violation. This manifests not only in violation
719 duration, but also in any internal temporal state.

720 5.3. Variable Duration Properties

721 In the LTL_f encoding of properties, any durations required of the prop-
722 erty are measured by counting a number of consecutive frames. Counting a
723 duration of N frames thus requires N separate states as each state encodes
724 its position in the sequence. This limits expressiveness as this number must
725 be determined as a part of the property specification and cannot be dynamic
726 in response to the system state. Consider § 46.2-849.B. from the Virginia
727 Driving Code on turn signals that says “Wherever the lawful speed is more
728 than 35 miles per hour, such signals shall be given continuously for a distance
729 of at least 100 feet, and in all other cases at least 50 feet, before slowing down,
730 stopping, turning, or partly turning” [17]. While SGSM could monitor for
731 whether the turn signal is being given continuously until the turn, it cannot
732 be used to track the required distance. A stricter version of the specification
733 could be encoded that leverages the fact that at 35 miles per hour it takes
734 1.95 seconds to travel 100 feet, and less time than that at higher speeds.
735 Thus, a property that monitors for 1.95 seconds would guarantee that no
736 violations occur, but if ego is travelling at 70 miles per hour will enforce a
737 duration that is twice as long as necessary. A richer logic is required to enable
738 connecting the temporal aspects of the monitor with the dynamic aspects of
739 the system; we leave such exploration to future work.

740 5.4. Precision and Recall of Scene Graph Generators

741 The foundation of SGSM entails the use of SGs to capture the relevant
742 information about the AV and its environment which SGL++ then uses to
743 extract the relevant APs to monitor the properties. While SGs are an ex-
744 tensible framework with the potential to encode arbitrary entities, relations,
745 and attributes, in practice there are limits to the SGs due to the precision

746 and recall of modern SGGs. To this end, the set of specifications that can
747 be accurately checked are limited by the SGGs employed during monitor-
748 ing. Modern SGGs rely on state-of-the-art object detection methods such as
749 Detectron2 [54], etc. to identify entities. Such rich perception systems are
750 still an active field of research, and current methods have limited precision,
751 particularly when evaluating over less common classes [73]. A prior limited-
752 scale study of SGGs over real data showed that for only 60% of images did
753 the SG produced match a human annotation [19]. An inaccuracy in the SG
754 could lead to an incorrect AP as evaluated by the monitor which could lead
755 to erroneous or missed violations or violation recoveries. Such inaccuracies
756 could arise from, e.g., an erroneous inclusion or exclusion of an entity, mis-
757 labeling of an attribute, or an incorrectly defined edge We hypothesize that
758 adding a notion of uncertainty or confidence to both the properties and the
759 SGG to enable, e.g., “the vehicle must stop if it is 50% sure there is a stop
760 sign” would aid in this aspect; however, accurately judging confidence and
761 integrating uncertainty across sensor and perception modalities remains a
762 challenge that we leave for future work.

763 The set of specifications that can be checked by existing SGGs is also
764 limited by the range of available entities, attributes, and relations of the
765 SGG. Consider § 46.2-828.1 of the Virginia Driving Code which states “It
766 shall be unlawful for [...] any motor vehicle intentionally to impede or disrupt
767 a funeral procession” [17]; unless the SGG has a mechanism for perceiving
768 and annotating a funeral procession in the SG, this remains out of reach for
769 runtime monitoring. The space of entities, attributes, and relations described
770 in the driving code and other sources for AV safety properties should serve
771 to inform the development of future SGGs.

772 6. Study

773 We aim to answer the following research questions:

774 RQ#1: What driving properties can SGSM express?

775 RQ#2: Can SGSM find safety violations in AV systems?

776 RQ#3: Can SGSM++ identify the count and duration of violations?

777 *6.1. Setup*

778 To evaluate SGSM++’s performance in contrast to SGSM’s ability to act
779 as an automatic safety monitor, we need a common execution environment
780 on which to run several AV systems to monitor.

781 *6.1.1. Common Execution Platform*

782 For running the study, we used the CARLA simulator for urban driv-
783 ing [21], which is widely-targeted for AV development due to its realistic
784 environments, complex traffic simulation, and ability to model a variety of
785 relevant road scenarios. CARLA holds a competition called the Autonomous
786 Driving Leaderboard, which provides preconfigured scenarios to challenge the
787 community to create systems that can drive autonomously. The challenge
788 includes a variety of towns, 10 different scenarios, each one of them defining
789 a different traffic situation, and a set of routes. We evaluated the 3 top-
790 ranked systems [74] as of June 2022, using the provided evaluation routes for
791 Town05, that includes 2-lane roads and 3-lane highways; 4-lane and T inter-
792 sections; traffic lights, stop signs, crossing lanes; and pedestrians, cyclists,
793 cars, and trucks. Particularly relevant to the properties examined later in
794 the study, the evaluation routes pass 27 stop signs and 109 junctions.

795 We developed an SGG in the form of a Python module that interfaces
796 with the CARLA API to extract the relevant entities, their attributes, and
797 compute their relationships with each other and the road structure. The SGG
798 uses ground truth information from CARLA to include all entities within
799 a 50m by 50m area horizontally centered on ego and vertically offset to
800 include 45m ahead of ego to be consistent with prior work [18, 19]. We
801 adopt the default entity and relationship scheme from prior work on SGs for
802 AVs [56, 19], enriched with additional information to include entities for the
803 lanes, roads, and junctions and their relations based on the flow of traffic.
804 Our unoptimized SGG and annotator take on average 288 ms to create a
805 single SG* and our monitor takes 67 ms to evaluate all properties on it using
806 an Intel Xeon Silver 4216 CPU @ 2.10GHz, 128 GB of RAM, and one Nvidia
807 Titan RTX. While our simulation-based SGG uses ground truth information
808 to eliminate the effects of sensor noise in our study, the current trajectory
809 of SGG research in conjunction with the availability of HD maps for AV
810 systems is promising for implementation of SGSM and SGSM++ on real-
811 world systems.

Table 1: Properties implemented in SGL [18] and SGL++

ψ	VA Code	English Summary of Property	LTL _f Formula over SG propositions	# DFA States
ψ_1	§ 46.2-804	Ego vehicle cannot be in the opposing lane.	$\mathcal{G}(\neg isOppLane)$	2
ψ_2	§ 46.2-802	Ego vehicle cannot be out of the road.	$\mathcal{G}(\neg isOffRoad)$	2
ψ_3	§ 46.2-802	If ego vehicle is in the right-most lane, then ego vehicle should not steer to the right.	$\mathcal{G}(isInRightLane \wedge \neg isJunction \rightarrow isNotSteerRight)$	2
ψ_4	§ 46.2-816	Ego vehicle should not be behind another entity in the same lane whithin 4 meters while travelling at a speed $> S$.	$\mathcal{G}(isNearColl \rightarrow \neg isFasterThanS)$	2
ψ_5	§ 46.2-816	If ego vehicle is between 4 and 7 meters of the closest vehicle in the same lane and then comes within 4 meters of a vehicle in the same lane, throttle must not be positive.	$\mathcal{G}((isSuperNear \wedge \neg isNearColl) \wedge \mathcal{X}(isNearColl) \rightarrow \mathcal{X}(isNoThrottle))$	3
ψ_6	§ 46.2-888	If the ego vehicle is moving and there is no entity in the same lane as the ego vehicle within 7 meters, and there is no red traffic light or stop sign controlling the ego vehicle's lane, then the ego vehicle should not stop.	$\mathcal{G}(\neg isStopped \wedge \neg (isSuperNear \vee isNearColl) \wedge \neg hasRed \wedge \neg hasStop \wedge \mathcal{X}(\neg (isSuperNear \vee isNearColl) \wedge \neg hasRed \wedge \neg hasStop) \rightarrow \mathcal{X}(\neg isStopped))$	2
ψ_7	§ 46.2-804	If ego vehicle is not in a junction, then ego vehicle cannot be in more than one lane for more than T seconds (N samples).	$\neg \mathcal{F}\$[N][isMultipleLanes \wedge \neg isJunction]$	$N+1$
ψ_8	§ 46.2-833	Ego vehicle must exit junctions within T seconds (N samples).	$\neg \mathcal{F}\$[N][isOnlyJunction]$	$N+1$
ψ_9	§ 46.2-821	Once the ego vehicle detects a new stop signal controlling its lane, it must stop before passing the stop signal.	$\mathcal{G}((\neg hasStop \wedge \mathcal{X}(hasStop)) \rightarrow (\mathcal{X}(hasStop \mathcal{U} (isStopped \vee \mathcal{G}(hasStop))))))$	4

Table 2: Intermediate variables used in Atomic Propositions shown in Table 3

Name	SGL expression
<i>egoLanes</i>	$relSet(Ego, isIn)$
<i>egoRoads</i>	$relSet(egoLanes, isIn)$
<i>egoJunctions</i>	$relSet(egoRoads, isIn)$
<i>oppLanes</i>	$relSet(egoLanes, opposes)$
<i>offRoad</i>	$filterByAttr(egoLanes, kind, \lambda x : x = offRoad)$
<i>rightLanes</i>	$relSet(egoLanes, toRightOf)$
<i>steerRight</i>	$filterByAttr(Ego, steer, \lambda x : x > 0)$
<i>inEgoLane</i>	$relSetR(egoLanes, isIn) \setminus \{Ego\}$
<i>nearColl</i>	$relSet(inEgoLane, near_coll)$
<i>superNear</i>	$relSet(inEgoLane, super_near)$
<i>egoFasterS</i>	$filterByAttr(Ego, speed, \lambda x : x > S)$
<i>noThrottle</i>	$filterByAttr(Ego, throttle, \lambda x : x < \epsilon)$
<i>tLights</i>	$filterByAttr(G, kind, \lambda x : x = trafficLight)$
<i>redLights</i>	$filterByAttr(tLights, lightState, \lambda x : x = Red)$
<i>trafLightLns</i>	$relSet(redLights, controlsTrafficOf)$
<i>stopSigns</i>	$filterByAttr(G, kind, \lambda x : x = stopSign)$
<i>stopSignLanes</i>	$relSet(stopSigns, controlsTrafficOf)$
<i>egoStopped</i>	$filterByAttr(Ego, speed, \lambda x : x < \epsilon)$
<i>juncRoads</i>	$relSetR(egoJunctions, isIn)$

812 *6.1.2. AV Systems Evaluated*

813 Each AV takes in a list of waypoints from the route and produces at each
814 frame a control for steering, throttle, and brake; each system has different
815 sensors and software. **Interfuser** [75] consists of a Deep Neural Network
816 (DNN) with a transformer [76] architecture, and a controller that generates a
817 set of actions for ego. It takes 3 images from 3 RGB cameras and a cropped
818 center image to focus on distant traffic lights, a LiDAR point cloud, and
819 the GPS coordinates and computes a set of waypoints, an object density
820 map, traffic light state, stop sign presence, and if the vehicle is in a junction.
821 These are fed into the controller to produce the output. **TCP** [77] takes in 1
822 image from an RGB camera, ego’s speed, and the GPS coordinates and uses
823 a DNN composed of a CNN-based image encoder using ResNet34 [78], and
824 two GRU [79] branches for trajectory and control predictions. **LAV** [80]
825 consists of a perception DNN, motion planner, and controller. The DNN
826 consumes 3 images from 3 RGB cameras and a LiDAR point cloud, and
827 outputs a BEV map which is fed to the planner along with the next waypoint

Table 3: Atomic Propositions

Atomic Prop.	SGL expression
<i>isJunction</i>	$ egoJunctions > 0$
<i>isOppLane</i>	$ oppLanes > 0$
<i>isOffRoad</i>	$ offRoad > 0$
<i>isInRightLane</i>	$ rightLanes = 0$
<i>isNotSteerRight</i>	$ steerRight = 0$
<i>isNearColl</i>	$ nearColl > 0$
<i>isFasterThanS</i>	$ egoFasterS = 1$
<i>isSuperNear</i>	$ superNear > 0$
<i>isNoThrottle</i>	$ noThottle = 1$
<i>isMultipleLanes</i>	$ egoLanes > 1$
<i>hasRed</i>	$ trafLightLns \cap egoLanes > 0$
<i>hasStop</i>	$ stopSignLanes \cap egoLanes > 0$
<i>isStopped</i>	$ egoStopped = 1$
<i>isOnlyJunction</i>	$ egoRoads \setminus juncRoads = 0$

828 coordinates to produce the next 10 future waypoints. The waypoints are
 829 passed to the controller along with a braking signal from a binary DNN
 830 classifier to compute the output.

831 6.2. RQ#1. SGSM Properties Evaluated

832 To evaluate SGSM’s ability to encode safe driving properties relevant to
 833 AV systems, we selected 9 properties from the laws and best practices of the
 834 Virginia Driving Code [17]. Laws were selected to yield a set of properties
 835 within scope of current AV systems and diverse in both temporal aspects
 836 required to analyze the property compliance and richness of the SG structure
 837 required to evaluate the APs.

838 Table 1 shows the successful encoding of those properties, with their
 839 relevant statute, a short English summary, and their encoding using the APs
 840 over the SG* composed through the LTL_f formula. Additionally, the number
 841 of states in the DFA is shown as a measure of temporal complexity. We note
 842 that precisely encoding the semantics of the law is challenging. Returning
 843 to the stop sign example, the APs are evaluated over the LTL_f formula to
 844 track if *isStopped* is true at least once between *hasStop* becoming true and
 845 later becoming false, indicating that ego stopped while being controlled by
 846 the stop sign. This is a necessary but insufficient specification to meet the
 847 criteria under the law; notably, this does not check that the vehicle stopped
 848 *at the stop line* rather than before, nor does it enforce separate stops for

849 successive stop signs along the same lane.

850 As ψ_4 , ψ_7 , and ψ_8 contain a threshold parameter, we instantiate 3 versions
 851 of each, for a total of 15 monitors. For ψ_4 , $S \in \{5, 10, 15\} \frac{m}{s}$ was chosen to
 852 represent parking-lot, urban, and suburban driving speeds. For ψ_7 , empirical
 853 studies found that lane changes take 4.6s on average with a std dev of 2.3s
 854 and max of 13.3s [81]; thus we select $T \in \{5, 10, 15\}s$ to represent the average,
 855 2 std dev, and beyond max. For ψ_8 , we select $T \in \{5, 10, 15\}s$ as the time to
 856 clear the intersection as a left turn across a 4 lane road at 10mph takes 5s,
 857 and we allow for a buffer factor of $1 - 3\times$.

858 We note that while some parameters can be expressed in SGL, others are
 859 reliant on the parameterization of the underlying SGG. In ψ_4 , ψ_5 , and ψ_6 , we
 860 use 4 and 7 meters as the distance thresholds because these correspond to the
 861 ‘near collision’ and ‘super near’ relationship used by prior AV SGGs [56, 19].
 862 Further, the underlying laws do not provide concrete values, e.g. the law
 863 from ψ_5 says “[...] a motor vehicle shall not follow [a vehicle] **more closely**
 864 **than is reasonable and prudent** [...]” (emphasis added) [17].

Table 4: 20 Sections Randomly Selected from the Virginia Driving Code [17]

Applicable to ego	Expressible by SGSM	Count	Sections
No	N/A	10	808, 819.3:1, 819.9, 831, 866, 873, 876, 882.1, 895, 926
Yes	Yes	7	817, 826, 834, 836, 862, 902, 903
	No	3	816.1, 854, 921

865 When examining the driving code [17] we find that our framework,
 866 equipped with additional entities and attributes, can already encode many
 867 additional rules. For example, § 46.2-803, 805, and 807 are all variations
 868 on the theme of § 46.2-804 about where the vehicle can operate checked by
 869 ψ_1 for different situations, e.g. in traffic circles. Similarly, § 46.2-833, 835,
 870 and 836 describe how vehicles must respond to traffic lights. These can be
 871 encoded similarly to § 46.2-821 for stopping at stop signs as checked by ψ_9 .

872 However, to obtain a more quantitative grasp of the expressiveness of the
 873 DSL, we randomly sampled 20 sections, shown in Table 4, of the 207 sections
 874 of the driving code chapter on the regulation of traffic [17]. Of these, we
 875 found that 10 applied to AVs while the other 10 were either targeting other
 876 non-AV entities, e.g. pedestrians, or covered bureaucratic administration of
 877 the code. Of the 10 applicable to AVs, we find that 7 can be encoded through

878 SGSM, though some require richer SGs than examined in our implementa-
 879 tion. For example, § 46.2-817, 834, and 902 concern the AV responding to
 880 signals from law-enforcement officers directing traffic. If the SGG could iden-
 881 tify law-enforcement officers as entities in the SG and interpret signals from
 882 the officer as a relationship between the officer and ego, then SGSM can en-
 883 code these sections. Of the 3 sections that cannot be encoded in SGSM, one
 884 section, § 46.2-816.1, cannot be encoded directly because it does not con-
 885 tain sufficient specificity—the section targets “careless or distracted” driving
 886 leading to injury; fully and formally specifying this section is beyond the
 887 scope of SGSM and likely generally intractable. The remaining two sections
 888 that cannot be encoded concern passing (§ 46.2-854) and following (§ 46.2-
 889 921) other vehicles. These sections cannot be encoded due to the limitation
 890 of symbolic entities described in Section 5.1 as passing or following a spe-
 891 cific vehicle requires tracking that same vehicle through time. Overall, this
 892 analysis highlights the expressiveness of SGSM and its utility for the task of
 893 runtime monitoring of safety properties, with SGSM able to encode 70% of
 894 the applicable properties in this sample.

RQ# 1 Findings: SGSM is able to successfully encode a wide variety of safety properties, with this study demonstrating the successful encoding of 9 properties from the driving code. Further analysis shows that this generalizes to additional properties based on entities and their relationships, showing the potential of SGSM to express many safety driving properties.

895

896 *6.3. RQ#2. Violations Observed*



(a) Interfuser violates ψ_1 . Missed road curve, and crossed into opp. lane.



(b) LAV violates ψ_2 . Left turn missed lane and drove into median.

Figure 6: Interfuser and LAV safety violations identified with SGSM [18].

897 As described in RQ#1, we derive 15 properties from the Virginia Driving
 898 Code and use SGSM to implement a monitor for each property. We ran each

899 AV system through the 10 evaluation scenarios of the CARLA leaderboard
900 and separately evaluated all 15 properties at a rate of $2Hz$.

901 Table 7.1 (left-most set of columns) shows how many of the 10 routes con-
902 tained at least one violation for each AV system for each of the properties.
903 Note that since the properties are defined as global properties, i.e. once a
904 violation occurs it reaches a trap state, we can track only the first violation,
905 for a maximum of 10 possible violations per AV system per property. We
906 find that the number of violations ranges from 51 for TCP to 72 for Inter-
907 fuser (over 150 possible violations). Fig. 6a shows an instance of Interfuser
908 violating ψ_1 ; as the road curved to the right, Interfuser did not steer right
909 enough and drifted into the opposing lane. Fig. 6b shows LAV violating
910 ψ_2 , turning left through a junction too sharply, exiting the junction into the
911 median between two lanes. While this is not off of the road bed, the SGG
912 denotes it as off road because it is not part of a defined lane of traffic. Fig. 2
913 shows TCP violating ψ_9 over a series of frames. TCP approaches a junction
914 with a marked stop line, but it does not stop and enters the junction.

915 The property violation statistics also give insights into the driving style of
916 the AVs. None of the AVs violated ψ_4 , meaning that they maintained suffi-
917 cient follow distance from lead vehicles. However, we also see that Interfuser
918 and TCP violated ψ_6 over more than half the routes, i.e., they stopped in
919 the middle of the roadway. While we do observe 9 cases where this stoppage
920 is unjustifiable, in 4 other cases we observe that the AV is stopping due to a
921 stopped vehicle ahead of it but farther than the 7 meters prescribed in ψ_6 ,
922 and in the remaining 4 cases there is a traffic light that is transitioning out of
923 red. This highlights the difficulty in concretizing the parameters used in the
924 specification given the imprecise definitions in the driving manual; 7 meters
925 may be acceptable depending on circumstances. This is further shown in
926 the performance across the parameterizations of ψ_7 and ψ_8 . As T increases,
927 the specification is more relaxed which leads to fewer violations; e.g. TCP
928 reduces from 8 routes with violations to 0 under ψ_8 when T is increased from
929 5 to 10. Although TCP eliminates all violations, Interfuser and LAV do not
930 improve as rapidly. This may point to different AV’s optimizations; they
931 likely did not optimize for junction crossing times, and instead may have
932 prioritized moving cautiously through a junction leading to slower transits.

933 We note that while ψ_3 has an extremely high violation rate with 100%
934 of routes yielding at least one violation, this may point to a weakness in
935 the implementation of ψ_3 rather than of the AVs tested. As discussed in
936 Table 1, ψ_3 says that if ego is in the rightmost lane then it should not

937 steer to the right. The underlying goal of this property is that ego should
938 stay on the roadway and since the rightmost lane necessarily means there
939 is no additional roadway to the right. Thus, the property requires ego to
940 not turn right at all in these cases. However, this is very restrictive and
941 neglects the myriad of cases when turning right could be correct, e.g., if the
942 road is curving to the right. Future refinements of this implementation may
943 consider an adjustment of the property to instead require that ego steer no
944 sharper right than the road is curving right; however, the existing SGG does
945 not annotate the roadway with a notion of curvature, so this information is
946 not currently available at execution time. This highlights the importance to
947 align the property semantics, encoding, and SGG to ensure that reported
948 violations accurately reflect violations of the underlying driving property.

949 Overall, this highlights three features of SGSM. First, it showcases how it
950 enables the specification and monitoring of driving properties that included
951 entities like *lanes*, *vehicles*, and *traffic signals*; their attributes like *speed*
952 and *color*; and their relations like *is in*, *controls*, and *opposes*. Second, it
953 shows how SGSM can be parameterized to support a rich set of property
954 types, from stateless to temporal, over propositions that are easily accessible
955 through the scene graph. Third, it provides evidence of SGSM’s generality
956 as per its direct application to monitor three distinct systems.

RQ# 2 Findings: SGSM is able to operate as a safety monitor to identify property violations at runtime in a blackbox manner. Unlike prior approaches, SGSM is able to operate end-to-end, from sensors to actions, without assuming that certain high-level data is available. As applied to monitor three state-of-the-art research prototype AV systems, SGSM identified that the AVs violated 71% of the encoded safety properties.

957

958 6.4. RQ#3: SGSM++ Violation Counts and Durations

959 Table 5 and Table 6 show the recovery criteria and reset mapping respectively
960 for each of the properties studied which enable us to investigate the
961 count and duration of violations. In their simplest form, each of the studied
962 properties have recovery criteria that emit a DFA with no more than two
963 states; however, the framework is general to handle arbitrarily complex re-
964 recovery criteria. For example, consider a more advanced version of ψ_1 that
965 focused on aggressive or reckless driving. Virginia Driving Code §46.2-868.1

Table 5: Recovery Criteria encoded with SGSM++

Property	SGL++ Recovery Criteria
ψ_1	$isOppLane \ \mathcal{U} \ \neg isOppLane$
$\psi_1^{\$[30]}$	$\mathcal{F}\$[30][isOppLane]$
$\psi_1^{\$[60]}$	$\mathcal{F}\$[60][isOppLane]$
ψ_2	$isOffRoad \ \mathcal{U} \ \neg isOffRoad$
ψ_3	$\neg isNotSteerRight \ \mathcal{U} \ isNotSteerRight$
ψ_4	$(isNearCol \rightarrow isFasterThanS) \ \mathcal{U} \ \neg(isNearCol \rightarrow isFasterThanS)$
ψ_5	$\neg isNoThrottle \ \mathcal{U} \ isNoThrottle$
ψ_6	$isStopped \ \mathcal{U} \ \neg isStopped$
ψ_7	$\neg(\neg isMultipleLanes \vee isOnlyJunction) \ \mathcal{U}$ $(\neg isMultipleLanes \vee isOnlyJunction)$
ψ_8	$isOnlyJunction \ \mathcal{U} \ \neg isOnlyJunction$
ψ_9	$True$

Table 6: Reset Mapping encoded with SGSM++

Property	SGL++ Reset Mapping
$\psi_1, \psi_1^{\$[30]}, \psi_1^{\$[60]}, \psi_2, \psi_3, \psi_4, \psi_5, \psi_6, \psi_7, \psi_8$	$\neg \mathcal{F} \ \mathbf{last}$
ψ_9	$hasStop \ \mathcal{U} \ (\neg hasStop \vee \mathbf{last})$

966 states that “[...] guilty of aggressive driving if [...] violates one or more of the
967 following: §46.2-802 (ψ_2) [...] with the intent to harass, intimidate, injure or
968 obstruct.” Further, §46.2-852 states that “[driving] recklessly or at a speed
969 or in a manner so as to endanger the life, limb, or property of any person
970 shall be guilty of reckless driving.” In this case, a stronger recovery criteria
971 may be desired that, e.g., ensures that the vehicle has not crossed into the
972 opposing lane for a certain duration before it could be considered no longer in
973 violation. This would allow for the encoding of aggressive or reckless driving
974 in the form of, e.g., repeated swerving across the center line as one violation.
975 The recovery condition given by $\mathcal{F}\$[N][\neg isOppLane]$ will cause the violation
976 to end only when the AV has been not in the opposing lane for N consecutive
977 time steps. We investigate this property as $\psi_1^{\$[N]}$ for $N = 30$ (15 seconds)
978 and $N = 60$ (30 seconds).

979 Note that the recovery criteria sets the minimal number of steps required
980 for recovery and thus the minimal duration of all violations. This minimal
981 duration is exactly the length of the shortest path between the initial state
982 and the accepting state of the DFA emitted by the recovery criteria. In the
983 case of the automatic recovery given by the condition $True$, this distance is

984 zero since the initial state is also the accept state. For the single condition
985 criteria described in Section 4.2 given by a $\mathcal{U} \neg a$, this distance is one since,
986 on the step that the property was violated, the condition a was *True*, so
987 it must take at least one step for a to be *False*; this can be seen visually
988 in the lower half of Fig. 5 for ψ_1 . In the more involved case about reckless
989 driving, the distance and thus minimal duration is N . This minimal duration
990 is important to consider when interpreting the results and comparing across
991 properties, e.g. for large values of N a violation of duration N may appear to
992 be poor behavior in absolute terms but actually be optimal for that particular
993 property violation.

994 Whereas Table 7.1 shows the number of routes with at least one vio-
995 lation, Table 7.2 (middle-left) shows the total number of violations across
996 all routes. Further, Tables 7.3 (middle-right) and 7.4 (right-most) show the
997 total duration over all violations, and maximum duration of any single vio-
998 lation respectively in terms of the number of frames over which the violation
999 persisted. Each frame is 0.5 seconds.

1000 First, by comparing Table 7.1 and Table 7.2, we see that almost all prop-
1001 erties are violated more than once on at least one route since the total count
1002 of violations is greater than the number of routes that had a violation. For
1003 some cases, this is markedly so as in ψ_3 . As noted in Section 6.3, ψ_3 's imple-
1004 mentation is stricter than the underlying goal property; this is further made
1005 clear by the violation counts shown with over half ($823/1405=59\%$) of all
1006 violations observed across all properties coming from ψ_3 .

1007 Second, by examining the count and duration we can gain an even clearer
1008 picture of the differing driving styles, strengths, and weaknesses of the differ-
1009 ent AV systems. As noted in Section 6.3, Interfuser and TCP violate ψ_6 at
1010 least once in over half of the routes, indicating that they stopped for no rea-
1011 son. While the number of routes with a violation makes Interfuser and TCP
1012 seem similar with violations in 9 routes and 6 routes respectively, the count of
1013 violations paints a much clearer picture with Interfuser having 141 violations
1014 to only 24 for TCP, indicating a clear pattern of violation for Interfuser while
1015 TCP's may have been separate isolated incidents. Further, examining the
1016 duration of violations in Tables 7.3 and 7.4 shows that when TCP did violate
1017 ψ_6 it always recovered on the next frame; meanwhile, Interfuser spent almost
1018 6000 frames, just shy of a third of the 18133 total frames ($5812/18133=32\%$)
1019 stopped for no reason, an average of over 40 frames per violation. This be-
1020 havior appears to be a known weakness of Interfuser—examining its internal

1021 code, its controller² contains logic that tracks how long it has been stopped
1022 for and forces the AV to drive forward if it exceeds a predefined threshold of
1023 60 seconds which is very close to our observed maximum violation duration
1024 of 117 frames or 58.5 seconds. This behavior is also related to the longest du-
1025 ration violation observed, where Interfuser violates $\psi_7^{T=5}$ for 1110 frames or 9
1026 minutes and 15 seconds. Examining the data, we see that Interfuser stopped
1027 between lanes, and although it moved slightly at least every 58.5 seconds per
1028 the data for ψ_6 , it did not complete the transition between lanes—the test
1029 ended while the system was still in violation.

1030 An additional valuable use case for this data is the identification of weak-
1031 nesses common across SUTs. Whereas Table 7.1 shows that the SUTs fail to
1032 stop at a stop sign at least once in 70% of the routes, the results in Table 7.2
1033 show that the SUTs failed to stop at a combined 63 stop signs, with each
1034 SUT missing at least 20. As discussed in Section 6.1.1, the test routes have
1035 the SUT transit 27 stop signs in total; thus, the SUTs collectively failed to
1036 stop at 63/81=78% of all stop signs. This information helps to clarify that
1037 it is not simply a few problematic intersections that cause the SUTs to fail
1038 once or twice per route, but instead the SUTs demonstrate pervasive and
1039 consistent difficulty in stopping at stop signs.

1040 These data also provide us with a basis to evaluate the more complex reset
1041 criteria studied for ψ_1 that can be used for judging, e.g. reckless driving.
1042 Recall that ψ_1 checks if ego is in the opposing lane. Recovering from ψ_1
1043 requires ego to not be in the opposing lane for a single frame, while $\psi_1^{s[30]}$
1044 and $\psi_1^{s[60]}$ require ego to not be in the opposing lane for 30 and 60 frames,
1045 or 15 and 30 seconds, respectively. Examining the total number of violations
1046 shown in Table 7.2 for LAV, we see that for the increasingly strict reset
1047 criteria, the number of violations goes from 8 to 7 to 6. The drop from
1048 8 violations to 7 violations between ψ_1 and $\psi_1^{s[30]}$ indicates that there were
1049 two separate violations that were more than 1 frame apart but less than
1050 30 frames apart. Likewise, the drop from 7 to 6 between $\psi_1^{s[30]}$ and $\psi_1^{s[60]}$
1051 indicates violations that are greater than 30 but less than 60 frames apart.
1052 As noted in Section 4.2, the minimum recovery time of $\psi_1^{s[30]}$ is 30 frames;
1053 however, looking at the maximum recovery time for LAV in Table 7.4, it is
1054 75 frames, this is partially due to the second violation causing the 30 second
1055 count to reset, leading to a much longer duration of violation. This effectively

²https://github.com/pendilab/InterFuser/.../interfuser_controller.py#L262

1056 demonstrates SGSM++’s ability to both encode and measure these complex
1057 counting and duration properties.

RQ# 3 Findings: SGSM++ successfully extends the functionality of SGSM by enriching the understanding of violation to include both the count and duration of violation. This allows for fine-grained analysis to identify, e.g., that not only did the three SUTs cross into the opposing lane in 15 different tests, they did so a combined 19 separate times for a total duration of 39 seconds and a maximum duration of 9.5 seconds. This significantly improves the practical utility of SGSM++ to be used as a safety monitor in practice.

1058

1059 *6.5. Threats of validity*

1060 In this study we showed the feasibility of implementing SGSM and its
1061 utility for checking safety property specifications based on driving rules. The
1062 external validity of our results, however, is bounded by our use of simulation
1063 to create the SGs using ground truth data. Working in simulation enabled us
1064 to construct an SGG module that generates high-quality SG representations
1065 of the world to judge the cost-effectiveness of the framework as a whole, but
1066 we recognize that it will be necessary to consider SGGs using various sensor
1067 types and in the wild. The CARLA simulator used in our study may differ
1068 from other deployment scenarios, including other simulators based on its
1069 particular design goals; further analysis in varied simulation environments is
1070 needed to understand the generality of the framework. Moreover, CARLA
1071 suffers from the simulation-reality gap [82], so deploying the approach in the
1072 real world will be necessary to assess its true potential in the field. The re-
1073 sults do provide evidence of the SGSM viability for monitoring richer driving
1074 properties, but its violation detection effectiveness will depend on the qual-
1075 ity of the systems under test and the scenarios under which those systems
1076 are exercised. We explored 3 systems competing under a CARLA bench-
1077 marking challenge and a set of predefined scenarios. Pushing SGSM towards
1078 commercial systems and richer scenarios will also contribute to generalize
1079 the findings. Similarly, more complex domain properties including those in-
1080 volving the behavior of multiple entities over time should be specified and
1081 checked to further evaluate the expressiveness and generality of SGSM.

1082 The internal validity of our results is mainly affected by our implementa-
1083 tion of SGSM and by our interpretation and encoding of the properties. We

Table 7: Full Study Results for the SUTs Interfuser [75], TCP [77], and LAV [80].

SUT	7.1: # Routes with ≥ 1 Violation (RQ#2)				7.2: Total # Violations (RQ#3)				7.3: Total Duration (# Frames) (RQ#3)				7.4: Max Duration (# Frames) (RQ#3)				
	[75]	[77]	[80]	Sum	[75]	[77]	[80]	Sum	[75]	[77]	[80]	Sum	[75]	[77]	[80]	Max	
ψ_1	3	6	6	15	4	7	8	19	10	18	50	78	4	5	19	19	
$\psi_1^{S[30]}$	See RQ#3				4	7	7	18	126	221	243	590	33	34	75	75	
$\psi_1^{S[60]}$	See RQ#3				4	7	6	17	246	431	376	1053	63	64	148	148	
ψ_1	0	0	1	1	0	0	2	2	0	0	17	17	0	0	11	11	
ψ_2	10	10	10	30	127	239	457	823	2299	2016	4416	8731	238	97	145	238	
ψ_3	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	
$\psi_4^S=10$	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	
$\psi_4^S=15$	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	
ψ_4	3	2	3	8	3	2	5	10	18	27	13	58	14	25	4	25	
ψ_5	9	6	3*	18	141	24	11	176	5812	24	11	5847	117	1	1	117	
ψ_6	10	5	8	23	22	9	18	49	2237	160	344	2741	1110	55	65	1110	
$\psi_7^T=5$	5	3	6	14	9	3	9	21	2103	105	187	2395	1100	45	55	1100	
$\psi_7^T=10$	5	3	5	13	7	3	7	17	2027	75	110	2212	1090	35	45	1090	
$\psi_7^T=15$	10	8	10	28	43	25	66	134	1258	55	396	1709	608	8	40	608	
$\psi_8^T=5$	5	0	6	11	5	0	8	13	1090	0	55	1145	598	0	30	598	
$\psi_8^T=10$	5	0	1	6	5	0	1	6	1040	0	20	1060	588	0	20	588	
$\psi_8^T=15$	7	7*	7	21	20	23	20	63	0	0	0	0	0	0	0	0	
ψ_9	72	50	66	188	394	349	625	1368	18266	3132	6238	27636	5563	369	658	5727	
Sum	10	10	10	30	141	239	457	823	5812	2016	4416	8731	1110	97	148	1110	
Max																	

We identified and fixed an error in the infrastructure for scene graph generation used in prior work [18], which is why these numbers differ from the earlier report (3 used to be 2, and 7* used to be 8).

1084 worked extensively to review the findings from utilizing SGSM to understand
1085 and validate that the implemented properties over the SGs faithfully encoded
1086 the desired semantics of the specification. Yet, SGs are always an approx-
1087 imation of the real environment attenuated by the SGG through sensors,
1088 perception, and other implementation artifacts. As such, the scene graph
1089 could include additional entities, not include other entities, or mis-relate cer-
1090 tain entities relative to the real environment. For example, we identified a
1091 failure of the SG generation wherein the SGG consistently fails to accurately
1092 capture the stop sign for one of the intersections. As such, SGSM cannot
1093 monitor for violations of ψ_9 at that intersection, and the relevant results of
1094 Section 6.4 may under count the stop sign violations by 1 for each of the
1095 SUTs. We leave to future work investigating, characterizing, and improving
1096 the robustness of SGSM with respect to the effects of these approximations.
1097 To mitigate this threat we have released an artifact containing the relevant
1098 system and data.

1099 *6.5.1. Potential for Field Deployments of SGSM++*

1100 Two principle factors impact the potential application of SGSM++ in the
1101 real world as a runtime monitor: accuracy and efficiency of its implementa-
1102 tion. Our experimental design relied on using the CARLA simulator and its
1103 Python API; this allowed our study to produce high-quality SGs and gener-
1104 ate the SGs in a manner decoupled from the simulator’s internal timing. As
1105 discussed, these factors allowed us to examine the expressiveness and utility
1106 of SGSM++ in this initial exploration and limit our ability to reason about
1107 the potential impacts of SGSM++’s accuracy and timing. The accuracy of
1108 SGSM++ is solely affected by the accuracy of the SGG used. The ability
1109 of SGSM++ to meet the real-time requirements for field application are af-
1110 fected by the time required for the SGG to create the SG and the time for
1111 SGSM++ to evaluate the property over the SG.

1112 We first comment on the accuracy and efficiency of current SGGs. Prior
1113 research has conducted initial studies on the accuracy and timing of current
1114 research-prototype SGGs on real-world camera images [19]. This exploration
1115 found that only 60% of SGs were fully accurate in a small-scale study. Fur-
1116 ther, the time required for the SGG varied greatly based on the size of the
1117 image, ranging from just under 1 second per image for low-resolution images
1118 under 100,000 pixels to just over 5 seconds per image for HD images around 2
1119 million pixels on a system with 32 cores and 4 GTX1080Ti GPUs [19]. Over-
1120 all, this low accuracy, slow performance, and required hardware present sub-

1121 stantial obstacles for the implementation of SGSM++ using current SGGs.
1122 However, the SGG studied was a research prototype that was not intended
1123 for real-time application; we hope that our results will spur future research
1124 into optimizing SGGs for real-time application.

1125 As for the time SGSM++ takes to process the SGs and evaluate the prop-
1126 erties, as discussed in Section 6.1.1, initial evaluations showed that each SG
1127 took less than 100ms to process in our un-optimized Python implementation.
1128 This is very promising for real-time application of SGSM++ for runtime mon-
1129 itoring as it indicates that the approach adds a proportionally small overhead
1130 compared to generating the SGs themselves. We believe that improvements
1131 in the SGG, as shown in recent benchmarks [30, 31], and optimizations in
1132 the monitor implementation could push these times to be practicable for
1133 application as a real-time monitor.

1134 7. Conclusion

1135 Providing assurances that AVs abide by safe driving properties is key
1136 to their successful deployment. However, specifying and monitoring such
1137 properties is challenging as they involve reasoning about not only the AV
1138 but also its relationship with other entities in the real environment, and
1139 such information is not readily accessible. Our previous work introduced the
1140 Scene Graph Safety Monitoring (SGSM) framework to better support the
1141 specification of safe driving properties and their automatic synthesis into an
1142 AV runtime monitor to detect and characterize property violations. In this
1143 work, we provide further analysis and formalization of SGSM and extend the
1144 framework to produce SGSM++, which captures the semantics of resetting a
1145 property violation, allowing the monitor to count the quantity and duration
1146 of violations. The study shows the expressiveness of the DSL for specifying
1147 9 real driving properties including the ability to reset these properties for
1148 continuous monitoring and the potential for generalization to a broad range
1149 of safe driving properties. The study further demonstrates the generality
1150 of the monitoring mechanism through its application to 3 off-the-shelf AV
1151 systems where it uncovers various driving violations. We find that these AV
1152 systems together violate 71% of the properties at least one time, including
1153 almost 1400 unique violations over 30 test executions, with violations lasting
1154 up to 9.25 minutes; additionally, the AVs fail to stop at stop signs in 78% of
1155 cases.

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